# SURFACE STRUCTURE AND REDUCTION PROCESSES OF Ti DOPED CeO<sub>2</sub>: A ULTRA ACCELERATED QUANTUM CHEMICAL MOLECULAR DYNAMICS STUDY

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# Abstract

Ti doping in CeO<sub>2</sub> can be used to modify its reactivity with respect to the oxygen vacancy formation and the redox properties. In the present study, we have investigated the effect of Ti doping on CeO<sub>2</sub> surface and its reduction properties using ultra accelerated quantum chemical molecular dynamics (UA-QCMD) method. A substitution of Ce atom by Ti atom in the surface layer causes strong structural distortion in the surface and lower oxygen vacancy formation energy compared to the undoped surface. Dopant lowers the formation energy of the active oxygen vacancy in the surface, confirming the potential for the dopant to be used in CeO<sub>2</sub> based materials for catalysis or solid oxide fuel cells, where the oxygen vacancy formation energy is important. It was successfully demonstrated by UA-QCMD that H<sub>2</sub> molecule adsorbs more strongly on the Ti doped surface compared to the undoped surface, and it is resulted in the formation of water molecule creating oxygen vacancy on the surface at 573 K.

Keywords: Ceria, Quantum chemical molecular dynamics, Ti, Hydrogen

## Introduction

 $CeO_2$  is an important catalyst in various industrial and environmental applications such as a three-way automotive exhaust catalyst (TWC) [Diwell et al.], oxygen storage [Yao et al.], oxidation of hydrocarbons, CO and decomposition of alcohol, and aldehydes. To understand the catalytic properties of both pure  $CeO_2$  and metal/ $CeO_2$  materials, it is imperative to examine the redox surface chemistry. It is capable of oxygen uptake and releases during excursions of the air/fuel mixture into the net oxidizing and reducing regimes, respectively. Recently, these materials have generated great interest in the solid

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oxide fuel cells as an alternative electrolyte for a lower temperature operation [Hibino et al.]. In the related field of "on board" hydrogen production via stream reforming of hydrocarbons, CeO<sub>2</sub>-based catalysts are currently being considered to facilitate low temperature water gas shift-gas reaction, which convert CO and water to  $CO_2$  and hydrogen. Most of these technological applications are based on the distinctive feature of Ce ions to easily switch oxidation states between +4 to +3.

It is generally known that one of the major deactivation pathways for TWCs is a result of shrunk the oxygen storage capacity (OSC) capabilities due to aging of the CeO<sub>2</sub> at high temperatures. It is therefore preferable to upgrade new CeO<sub>2</sub>-based materials with both high redox activity (large OSC) and high thermal resistance. Many efforts regarding the improvement of the promoter performance in the three-way catalyst at high temperatures have been found that mixing with zirconium oxide immensely changes the reducibility and thermal stability of CeO<sub>2</sub> and demonstrated that the modified structures of CeO<sub>2</sub> by Ti dopant could significantly prevent the sintering of Au nanoparticles. In the CeOx/TiO<sub>2</sub> (110) systems, the Ce cations adopt a structural geometry and an oxidation state (+3) that are quite different from those seen in bulk CeO<sub>2</sub> or for CeO<sub>2</sub> is very weakly bound, with oxidation enthalpies even lower than that found with CeO<sub>2</sub>-zirconia solutions. Although the CeO<sub>2</sub>-titania solutions are not as stable as CeO<sub>2</sub>-zirconia solutions, they have properties that may make them useful for some catalytic applications

Yang et al. demonstrated that the Zr dopant can enhance the adsorption of CO and also may probably promote the desorption of  $CO_2$  molecule from the surface. They also discussed how the Zr doping changes the reduction and catalytic properties of  $CO_2$ .

The reduction of  $CeO_2$  and formation of oxygen vacancies have been characterized over recent years by both experiment and first principle simulations [Keating et al.]. The release and uptake of oxygen by  $CeO_2$  allow it to participate in redox reactions, such as CO oxidation to  $CO_2$  [Bedrane et al.] and NOx reduction. Over recent years a great deal of work has been devoted to examining how the reactivity of  $CeO_2$  can be improved [Yang et al.]. With the example of CO oxidation, it is understand that enhancing oxygen vacancy formation is important if this formation energy can be made smaller, then oxidative power of  $CeO_2$  will be improved and there are number of theoretical studies elaborating upon this idea, as well as experiments confirming this concept. Examples of dopants include Zr, La, Pd, Ti [Reddy et al.] and Cu.

Doping of  $CeO_2$  with other metallic elements, such as Zr, has been shown to enhance thermal stability and to promote catalytic activity. It is believed that doping facilitates the reduction of  $CeO_2$ , by weakening the bonds to the oxygen atoms around the dopant. A number of computational studies have demonstrated that the oxygen vacancy formation energy is lower when the surfaces is doped Zr, Pt [Nolan et al.]. Replacing a Ce atom on  $CeO_2$  surfaces enhances CO oxidation and the Ce-O and dopant-O bonds are weakened upon formation of the doped material with reducing the oxygen vacancy formation energy and enhance the reactivity of the surface. Most of the computational studies of doped  $CeO_2$  have investigated oxygen vacancy formation, with little work on molecular adsorption at the doped surface.

In this article, we use ultra accelerated quantum chemical molecular dynamics to study the effect of doping the (111) surface of  $CeO_2$  with Ti on H<sub>2</sub> adsorption and water desorption mechanisms. Recent experimental work has focused on  $CeO_2$  nanostructures that predominantly expose a particular surface, e.g. (111) on nanoparticle or (110) on nanorods. The earlier work has shown that the (111) surface can be made more favorable for oxygen vacancy by doping [Shapovalov et al.]. For the choice of dopant, there has been a recent experimental work related to Ti dopant in CeO<sub>2</sub>. This dopant has formal 4+ charge, therefore it involves charge compensation or oxygen hole formation processes. This work also allows comparison with previous work on H<sub>2</sub> adsorption at undoped CeO<sub>2</sub> surface [Alam et al.] and Ti doped CeO<sub>2</sub> surface as well as water desorption mechanisms and provides important information on the impact of doping during the redox reactions at CeO<sub>2</sub> surfaces.

#### **Computational Methods**

## a) Quantum Chemical Molecular Dynamics Method:

To investigate the atomic interactions between hydrogen on  $CeO_2$  surfaces, we used our in house code UA-QCMD [Alam et al.]. The program is based on a tight-binding quantum chemistry (TBQC) calculation program "New colors" [Alam et al.] and classical molecular dynamics (MD) program "NEW RYUDO" [Elanany et al.]. In the UA-QCMD program, the center of the chemical reaction and electrons transfer dynamics are calculated by TBQC and remaining part is calculated by MD, thus realizing the study of chemical reaction and electrons transfer dynamics for a complex system.

Dynamics of atoms were carried out using the following potential functions (eq.1), which were employed to consider the ionic, covalent, and weak van der Waals interactions among atoms.

$$U = \sum_{i} \sum_{j>1} \left[ \frac{Z_{i} Z_{j} e^{2}}{r_{ij}} + f_{0} (b_{i} + b_{j}) \exp \left( \frac{a_{i} + a_{j} - r_{ij}}{b_{i} + b_{j}} \right) - \frac{c_{i} c_{j}}{r^{\sigma}_{ij}} \right] + \sum_{i} \sum_{j>i} D_{ij} \left\{ \exp[\frac{1}{2} - 2\beta_{ij} (r_{ij} - r_{0})] - 2\exp[\frac{1}{2} - \beta_{ij} (r_{ij} - r_{0})] \right\}$$
(1)

The first term corresponds to the Coulomb potential, and the second term corresponds to the short-range exchange repulsion potential ( $f_0$  is the constant for unit adjustment, a is the size, and b is the stiffness), which gives a good account of the repulsive interactions arising from the overlap of electronic clouds. The third term represents van der Waals dispersive interaction (c is the constant for each atom). The fourth term in eq.(1) corresponds to the Morse-type potential, which represents covalent interactions, where  $D_{ij}$  is the bond energy,  $\beta_{ij}$  is the form factor, and  $r_0$  is the bond length at minimum energy. Using these potentials determined by the above-mentioned scheme, MD simulation was performed. In this MD, a Varlet algorithm is employed to integrate equation of motion. Moreover, the temperature scaling method implemented in the system is similar to the Woodcock algorithm.

Element	AO	$a_0$	$a_1$	$a_2$	$a_3$	$a_4$	$a_5$
Н	S	0.9484	1.5794	0.0000	0.0000	0.0000	0.0000
0	S	2.1450	0.0802	0.0185	0.0007	0.000	0.000
0	р	1.9664	0.5181	1.0817	1.1475	0.000	0.000
Ti	S	1.1868	0.2873	-0.0664	0.0347	0.0434	0.0048
	р	1.1091	0.0085	0.0041	0.0000	-0.0013	-0.0004
	d	1.6209	0.3323	-0.0017	-0.0202	-0.0004	0.0007
	S	2.7165	0.0332	0.0208	0.0041	0.0000	0.0000
Ce	р	2.7165	0.0010	-0.0127	0.0093	0.0000	0.0000
	d	3.1519	0.3368	0.0000	0.0000	0.0000	0.0000
	f	4.5582	0.3363	0.0000	0.0000	0.0000	0.0000

Table 1: Determined coefficient of a single  $\zeta$  parameter in a Slater-type atomic orbital in eq. (3)

In the TBQC, an electronic structure calculation was performed by solving the Schrödinger equation ( $HC = \varepsilon SC$ ; H, C,  $\varepsilon$ , and S refer to the Hamiltonian matrix, eigenvectors, eigenvalues, and overlap integral matrix, respectively) with the diagonalization condition ( $C^TSC = I$ ; I refers to the identity matrix). In the TBQC, the *Slater* type basis set was employed and long-range Columbic interactions were computed by the Ewald method. In order to determine the off-diagonal elements of H,  $H_{rs}$ , the corrected distance-dependent Wolfsberg-Helmholz formula eq. (2) was used;

$$H_{rs} = \frac{K}{2} S_{rs} \left( H_{rr} + H_{ss} \right) \tag{2}$$

Table 2: Determined coefficient parameters of  $H_{rr}$  parameterin eq. (4)

Element	AO	$b_0$	$b_1$	$b_2$	$b_3$	$b_4$	$b_5$
Н	S	-10.5503	-12.4348	-1.4354	0.0000	0.0000	0.0000
0	S	-28.6066	-15.0328	-1.4510	-0.4949	0.0419	0.0000
	р	-14.2851	-14.8159	-1.6244	0.0154	0.0434	0.0010
Ti	S	-7.4127	-7.1349	-0.9582	0.0364	0.000	0.0000
	р	-3.9812	-5.7018	0.0392	-0.1391	0.000	0.0000
	d	-8.0415	-7.4870	-0.6046	0.0349	0.000	0.0000
Ce	S	-5.5303	-5.0728	3.4414	-4.3070	1.5907	-0.1994
	р	-0.0612	-4.6247	3.8922	-4.4481	1.6406	-0.2082
	d	-8.4356	-4.8609	7.5711	-9.4497	3.5251	-0.4442
	f	-7.1929	-8.1663	3.1559	-1.5706	0.0885	0.0000

b) First-Principles Parameterisation in Tight-binding Calculation:

In order to set the Hamiltonian matrix H and overlap integral matrix S in our TBQC, exponents of a Slater-type atomic orbital (AO), denoted as  $\zeta_{r,r}$  and valence state ionization potentials (VSIPs) for the 1s AO of H atoms as well the 2s and 2p AOs of O atoms, 4d and 4f AOs of Ce atom sare necessary. The former parameters are used to calculate the S matrix and  $H_{rs}$  in equation (2). The latter ones are used for the diagonal element of  $H(H_{rr} \text{ or } H_{ss})$  in eq. (2). The relationship between  $H_{rr}$  and VSIP of r-th AO of the *i*-th atom  $(I_r^i)$  is described as  $H_{rr} = -I_r^i$ . In our UA-QCMD simulator, these are represented by the polynomial functions of atomic charges. The  $\zeta_r$ , and  $H_{rr}$  are calculated by the polynomial functions of atomic charges described by eqs. (3) and (4), respectively.

$$\zeta_{r} = a_{0} + \sum_{k=1}^{5} a_{k} \left( Z_{i} \right)^{k}$$
(3)

$$H_{rr} = b_0 + \sum_{k=1}^{5} b_k \left( Z_i \right)^k \tag{4}$$

In eqs.(3) and (4),  $Z_i$  corresponds to the atomic charge on the atom *i*. The parameters regarding  $\zeta_r$ , i.e.,  $a_0$ ,  $a_1$ ,  $a_2$ ,  $a_3$ ,  $a_4$ , and  $a_5$  in eq. (3) and regarding  $H_{rr}$ , i.e.,  $b_0$ ,  $b_1$ ,  $b_2$ ,  $b_3$ ,  $b_4$ , and  $b_5$  in eq. (4), were determined so as to reproduce the binding energies and electronic structures of a H<sub>2</sub>/CeO<sub>2</sub> (111) surface model obtained by DFT calculations, which are summarized in Tables 1 and 2, respectively and explained in the later section.

# c) Periodic density functional theory method:

The DFT calculations were also performed in order to validate the accuracy of our TBQC method. The DMol<sup>3</sup>code [Delley et al.] was used for the present purpose and double numerical basis sets with polarization functions (DNP) were employed. The parameters used in eqs. (3) and (4) were tuned comparing with DFT results (atomic charges, bond populations, atomic orbital populations and binding energies).

Element	Atomic charge		
	DFT	TBQC	
Ce	0.50	0.48	
0	-0.25	-0.24	
Ti	0.78	0.76	
0	-0.39	0.38	
Н	0.00	0.00	

# Table 3: Atomic charge of individual atoms obtained by DFT and TBQC.

The geometry optimization was performed using generalized gradient approximation (GGA) with Perdew-Burke-Ernzerhof (PBE) exchange-correlation function [Perdew et al.] was adopted for energy calculations. The charge population was analyzed by Hirshfeld method.

Alam et al.



# d) Model Preparation:

Fig.1 CeO<sub>2</sub> bulk model used in the validation of parameterization. Here is a white sphere represent as cerium atoms and red spheres represent as oxygen atoms.

CeO<sub>2</sub> is generally considered to be an ionic oxide. The (111) surface is a neutral stoichiometric plane so that no dipole moment is present upon cleaving. The slab model was 11.9 Å (twelve atomic layers) thick, with a 38.10 Å vacuum gap in the direction perpendicular to the surface. For calculations, we used a super cell that is a ( $3\times3$ ) expansion with 12 surface oxygen atoms, so that substitution of one surface Ce atom with the dopant gave an overall dopant concentration of 2.1% and formation of one oxygen vacancy gave a surface vacancy concentration of 8.5%, with an overall vacancy concentration of 1.04%. Upon introduction of the dopant and the vacancy, all layers except the bottom two were relaxed. H<sub>2</sub> molecule was adsorbed and relaxed at the doped surfaces in a number of configurations to probe the dependence of adsorption energy on the adsorption site.

Atomic pair	DFT	TBQC	
Ce-O	0.22	0.19	
H-H	0.88	0.87	

Table 4: Comparison of calculated bond populations of Ce-O and H-H from DFTand TBQC.

Method	Element	s [%]	p [%]	d [%]	f[%]
DFT/CASTEP	Ο	27.93	72.07		
	Ce	8.55	2.97	55.02	33.46
	Ti	2.94	6.61	90.44	
TBQC	Ο	27.92	72.07		
	Ce	8.84	2.880	54.70	33.53
	Ti	2.77	4.96	92.26	

Table 5: Comparison of atomic orbital population of individual species of CeO<sub>2</sub> bulk model and TiO<sub>2</sub> model calculated by DFT and TBQC

#### **Results and Discussion**

a) Validation of parameters used in UA-QCMD:

The accuracy of the parameters used is evident in the comparison of the atomic charges, bond populations, atomic orbital populations of the CeO<sub>2</sub> bulk model obtained by TB-QC and DFT. In order to validate the parameters shown in Tables 1, 2 and 3. A bulk model of CeO<sub>2</sub> as shown in Figure 1, containing 12 Ce atoms and 24 O atoms, was prepared. The cell parameters of the CeO<sub>2</sub> bulk model were fixed during the calculations, which are a = 7.65 Å b = 6.63 Å and c = 9.38 Å, and  $\alpha = \beta = r = 90^{\circ}$ . Hirshfeld atomic charges, found through DFT, were compared with the atomic charges obtained by the TBQC. Atomic charges of Ce, O, Ti and H atom obtained by DFT and TBQC were close to those found with DFT as shown in Table 1.

Table 2 shows the comparison of bond population of Ce-O and H-H pairs from TBQC which are in good agreement with those from DFT. Table 3 compares the ratios of atomic orbital populations for individual atoms, where the ratios of atomic orbital populations for each valence orbital obtained by TBQC were close to those obtained by DFT.

Alam et al.



Fig. 2 Pictures of model for  $CeO_2$  (111) surface doped with Ti. The dopant is the large gray sphere, Ce is white, and O is red. (a) Optimized structure of Ti doped  $CeO_2$  surface (top view) (b) optimized structure of Ti doped  $CeO_2$  surface (side view). (c) and (d) are the initial structure of Ti doped  $CeO_2$  surface model. (e) is the surface structure after the relaxation.

# b) Structure of the doped CeO<sub>2</sub> surfaces:

The relaxed surface structure for the doped (111) surface is shown in Figure 2 (a-e). The dopant is the gray sphere in the outermost layer in the each surface. The  $CeO_2$  (111) surface has seven-coordinated surface Ce and three coordinated surface O, with the Ce-O distances only slightly shortened over the bulk oxide at 2.36 Å. In discussing the surface structure, the surface atoms are those in the first atomic layer that terminate the surface,

the 2<sup>nd</sup> atomic layer contains Ce and dopant, and the 3<sup>rd</sup> atomic layer contains the oxygen. Due to doping, Ti moves off its initial lattice site (Figure 2(a-e)) and surface oxygen atoms nearest the dopant are notably displaced from its lattice site. This result shows short Ti-O distances of 1.91 Å and 1.97 Å and long pair 2.14 Å and 2.12 Å, compared to the Ce-O distances of 2.36 Å in the un-doped surface. The short Ti-O distances in the surface lead to the longer pair of Ce-O distances 2.47 Å and 2.59 Å. All involve the surface Ce atom nearest the dopant.

Dopant concentration in this study is very small and therefore we would expect a smaller distortion of the coordination in the optimized structure. Due to doping, Ti moves off its initial lattice site (Figure 2(a-e)) and surface oxygen atoms nearest the dopant are notably displaced from its lattice site. This result shows short Ti-O distances of 1.91 Å and 1.97 Å and long pair 2.14 Å and 2.12 Å, compared to the Ce-O distances of 2.36 Å in the undoped surface. The short Ti-O distances in the surface lead to the longer pair of Ce-O distances 2.47 Å and 2.59 Å. All involve the surface Ce atom nearest the dopant. Dopant concentration in this study is very small and therefore we would expect a smaller distortion of the coordination in the optimized structure. Here distortions to the surface structure in Ti doped CeO<sub>2</sub> are a result of the small ionic radius of Ti<sup>4+</sup> (0.62 Å) compared to the Ce<sup>4+</sup>(0.97 Å), and the unfavorable coordination environment in which the dopant is found.

# b) The effect of Ti doping on O vacancy formation energies:

Oxygen vacancies are pertinent in the defect chemistry of  $CeO_2$ . Oxygen vacancy defect can appear on the oxide surface or in the bulk and can strongly modify the electronic and catalytic properties of the oxide. It has been found that the reducibility of  $CeO_2$  is greatly enhanced by the dopants. We have already calculated oxygen vacancy formation energy  $(E_{vac})$  of first layer in the surface using the eq. (5).

$$E_{vac} = E(\text{TiCeO}_{2vac}) + E(1/2O_2) - E(\text{TiCeO}_2)$$
(5)



Fig. 3 Calculation model of  $Ti/CeO_2$ -H<sub>2</sub> system used for the UA-QCMD calculation. Left and right hand figures represent the side and top views of the model, respectively.

The formation of an oxygen vacancy near the dopant (which is the most favorable vacancy site, which is shown in Figure2).  $E(\text{TiCeO}_{2\text{vac}})$  is the total energy of the slab with the vacancy,  $E(\text{TiCeO}_2)$  is the total energy of the slab computed for the stoichiometric slab, and  $E(1/2O_2)$  is the computed binding energy for O atom. The oxygen vacancy formation energy on the surface of CeO<sub>2</sub> was estimated to be -66.64 kcal/mol. For Ti doping the formation energy is smaller than that of the un-doped surface, for which the energy of forming oxygen vacancy is computed to be -89.47 kcal/mol. Thus, doping of CeO<sub>2</sub> surface with Ti enhances the oxidative ability of the CeO<sub>2</sub> surface.

## d) H<sub>2</sub> adsorption on the doped surface:

In the calculation model in Figure 3 where the position of  $H_2$  molecule was set at most reactive site considering adsorption energy of different sites. Here lower part of the model was un-relaxed and upper part was relaxed. The calculation temperature was 573 K and the consecutive velocity of  $H_2$  molecule was 2700 m/s. The distance between  $H_2$ and the top region of CeO<sub>2</sub> surface is equivalent to 5.56Å. During the UA-QCMD simulation a snapshot at 40 fs (Figure 6.4 (b) shows that the  $H_2$  molecule comes approach to the surface where as a snap shot at 80 fs (Figure 4 (c) shows  $H_2$  molecule interacts with the surface oxygen at the reactive dopant site. In the gas phase, the bond distance of  $H_2$ 

was 0.74 Å and the bond information was changing while  $H_2$  molecule was approaching to the surface. Finally, when  $H_2$  molecule interacts with the surface, the bond length was lengthening from 0.74 Å to 0.80 Å. We investigate  $H_2$  adsorption on the doped CeO<sub>2</sub> surface. We have previously studied  $H_2$  adsorption at the un-doped CeO<sub>2</sub> surfaces [Alam et al.]. Here we wish to compare the details of  $H_2$  adsorption at the doped and un-doped surfaces, because this is the fundamental interaction involved in surface reduction processes of CeO<sub>2</sub>. The energy change upon  $H_2$  adsorption at the surface is calculated by

$$E_{ads} = E(\text{TiCeO}_2 + \text{H}_2) - [E(\text{TiCeO}_2) + E(\text{H}_2)] \quad (6)$$

 $E_{ads}$  is negative when the adsorbed H<sub>2</sub> is more stable than that in the gas phase. The adsorption energy of H<sub>2</sub> on the un-doped (111) surface is -28.7 kcal/mol, where as on the doped surfaces, the adsorption energy is -56.4 kcal/mol. Here the enhanced reactivity to H<sub>2</sub> adsorption arises because, upon adsorption on a CeO<sub>2</sub> surface, H<sub>2</sub> pulls surface oxygen atoms from the lattice site; the smaller oxygen vacancy energy, the more this process will be promoted and this results in the stabilization of the intermediate.

## e) Hydrogen dissociation and water desorption:

After the adsorption, $H_2$  molecule dissociated homolytically on the surface and formed two OH- groups as shown in Figure 4 (e). A notable difference was found between the doped and un-doped surfaces for hydrogen adsorption and dissociation processes. The ease with which oxygen can be removed from these surfaces allows an oxygen atom to be pulled farther from the surface than for the un-doped surface. The bond lengths of two OH groups were about 1.00 Å and also bond energies were about –95 kcal/mol. There is a mutual interaction occurred between OH groups and formed water molecule creating oxygen vacancy on the surface.



Fig. 4 Snapshot of the result from UA-QCMD calculation at different simulation steps from 0 to 480 fs: (a) Initial model of  $H_2/Ti/CeO_2$  (b-c) the snapshots at 40 and 80 fs where  $H_2$ approaches to the surface, (d)  $H_2$  adsorbed on the surface, (e)  $H_2$ was dissociated and formed OH groups, (f) is the snapshot at 250 fs where mutual interaction occurred between the OH groups. (g) shows one lattice oxygen atom about to desorbs from the surface. (h) is the snapshot at 480 fs where  $H_2O$  molecule completely desorbed from the surface.

Looking briefly at the surface, the dopant and neighboring Ce atom in the surface move apart, with the distortions in the surface and first subsurface layer that is shown in both views of the plan and the side in Figure 2. Figure 5 shows the changes of the bond length of adsorbing  $H_2$  and the reactive surface O during the simulation. In MD simulation hydrogen approached to the reactive sites and we have considered the variation of bond lengths with respect to time. Initial distance was 5.56 Å (average) desorbed from the surface with  $H_2$  atoms, the bond length changes to about 1.00 Å.



Fig. 5 Comparison of the change of the bond lengths between reactive oxygen (O) to H (a) and H (b) in  $H_2$  during the simulation. Red solid line (triangle) indicates the change of bond length between O-H (a) and broken line (circle) indicates the change of the bond length between O to H (b).

At around 250 fs when hydrogen completely adsorbed and dissociated on the surface the O-H bonds was about 0.98 Å and finally when one atom oxygen. From the inspection it was clarified that  $H_2$  adsorption, dissociation and desorption as a water molecule from the surface creates oxygen vacancy. The introduction of the dopant into the (111) surface of CeO<sub>2</sub> reduces the energy required for formation of an oxygen vacancy in the surface. The distortion of the atomic structure around the dopant site tends to weaken the Ce-O bonds and makes removal of oxygen easier. The adsorption of  $H_2$  onto the doped surface shows the impact of the reduction of the vacancy formation energy. Comparing the adsorption energy of  $H_2$  on the non-doped surface [Alam et al.] to the doped surface it is obvious that dopant makes the surface more reactive than that of un-doped surface.

# Conclusion

In this article, based on the theoretical studies involving quantum chemical molecular dynamics, we have demonstrated the surface reduction process of Ti doped  $CeO_2$  surface. We have analyzed the hydrogen adsorption, dissociation and water desorption mechanisms in case of Ti doped  $CeO_2$  surface and made a comparison with the properties of the non-doped case. It was shown that Ti doping enhances the oxidative power of the

oxide, as indicating by reduction energy required for the formation of oxygen vacancy and enhanced adsorption energy of  $H_2$ .

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